

3.7 Multiplying Polynomials

Lesson Focus

Extend the strategies for multiplying binomials to multiplying polynomials

Bigger than FOIL

To distribute a binomial multiplied by a binomial remember FOIL

F – (first)(first)

O – (outside)(outside)

I – (inside)(inside)

L – (last)(last)

$$(h + 11)(h + 5)$$

The distributive property can be used to perform any polynomial multiplication

Each term of one polynomial must be multiplied by **each term** of the other polynomial

Example

Expand and simplify.

a) $(2h + 5)(h^2 + 3h - 4)$

$$= \cancel{2h^3} + \cancel{6h^2} - \cancel{8h} + \cancel{5h^2} + \cancel{15h} - 20$$

$$= 2h^{\textcircled{3}} + 11h^2 + 7h - 20$$

Degree 3

constant

Example

Expand and simplify.

b) $(-3f^2 + 3f - 2)(4f^2 - f - 6)$

$$= -12f^4 + 3f^3 + 18f^2 + 12f^3 - 3f^2 - 18f - 8f^2 + 2f + 12$$

$$= -12f^4 + 15f^3 + 7f^2 - 16f + 12$$

Example – Your Turn

Expand and simplify.

a) $(3k + 4)(k^2 - 2k - 7)$

b) $(-2t^2 + 4t - 3)(5t^2 - 2t + 1)$

Example – More than 1 Variable

Expand and simplify.

a) $(2r + 5t)^2$

b) $(3x - 2y)(4x - 3y + 5)$

$$= (2r + 5t)(2r + 5t)$$

$$= 4r^2 + 10rt + 10rt + 25t^2$$

$$= 4r^2 + 20rt + 25t^2$$

$$\text{b) } (3x - 2y)(4x - 3y + 5)$$

$$= \cancel{12x^2} - \cancel{9xy} + 15x - \cancel{8xy} + 6y^2 - 10y$$

$$= 12x^2 - 17xy + 15x - 10y + 6y^2$$

$$(2r + 5t)^2$$

$$= 4r^2 + 20rt + 25t^2$$

Homework

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4a,c, 5b,d,f, 7a, 8

Example

Expand and simplify.

a) $(2c - 3)(c + 5) + 3(c - 3)(-3c + 1)$

$$\begin{aligned} &= 2c^2 + 10c - 3c - 15 + (3c - 9)(-3c + 1) \\ &= 2c^2 + 7c - 15 + (-9c^2 + 3c + 27c - 9) \\ &= \cancel{2c^2} + 7c - 15 - \cancel{9c^2} + 30c - 9 \\ &= -7c^2 + 37c - 24 \end{aligned}$$

Example

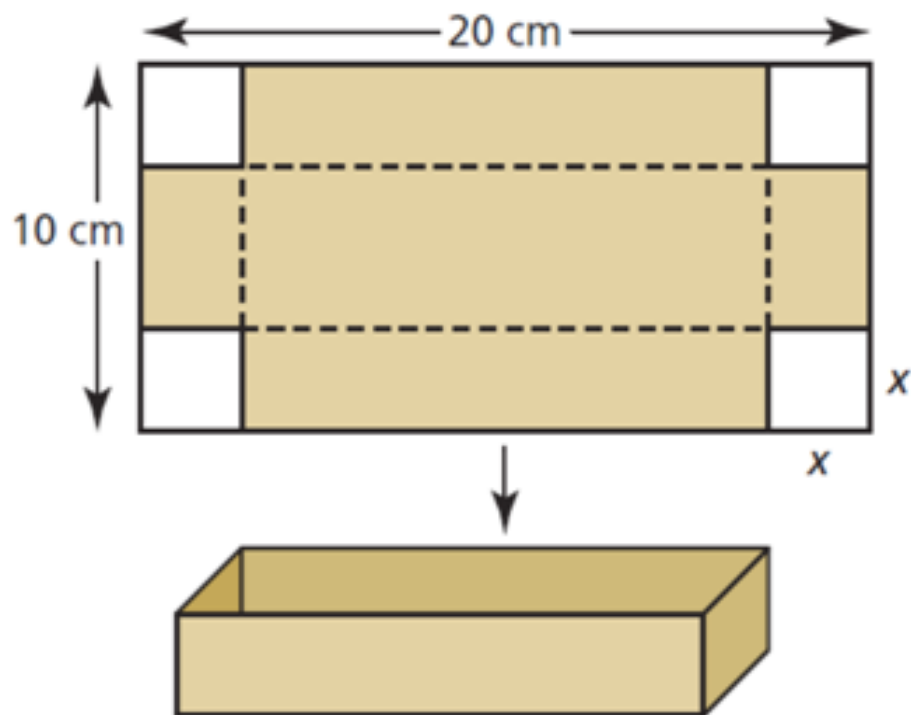
Expand and simplify.

$$\text{b) } (3x + y - 1)(2x - 4) - (3x + 2y)^2$$

$$\begin{aligned} &= \cancel{6x^2} - \cancel{12x} + \cancel{2xy} - \cancel{4y} - \cancel{2x} + \cancel{4} - (9x^2 + 12xy + 4y^2) \\ &= \cancel{6x^2} - \cancel{14x} + \cancel{2xy} - \cancel{4y} + \cancel{4} - \cancel{9x^2} - \cancel{12xy} - 4y^2 \\ &= -3x^2 - 14x - 10xy - 4y - 4y^2 + 4 \end{aligned}$$

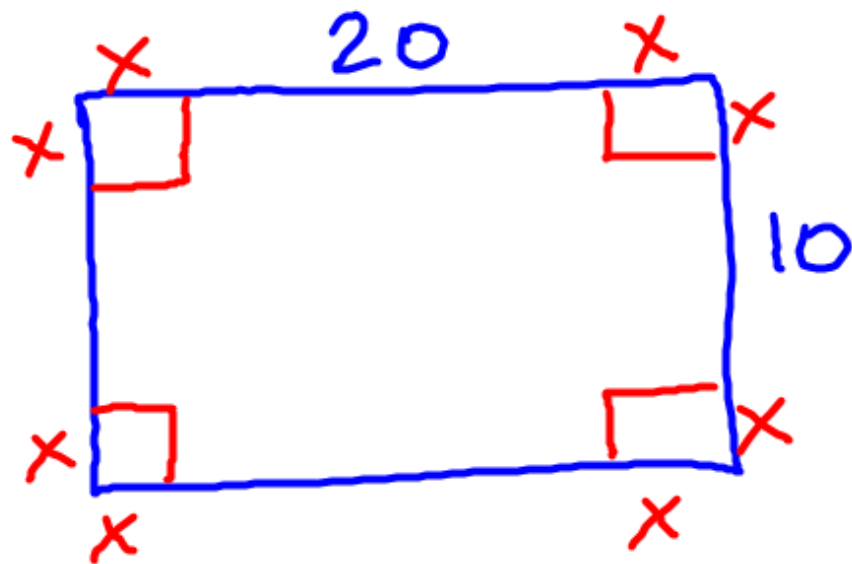
Example

A box with no top is made from a piece of cardboard 20 cm by 10 cm. Equal squares are cut from each corner and the sides are folded up.



Let x centimetres represent the side length of each square cut out. Write a polynomial to represent each measurement. Simplify each polynomial.

- the length of the box
- the width of the box
- the area of the base of the box
- the volume of the box

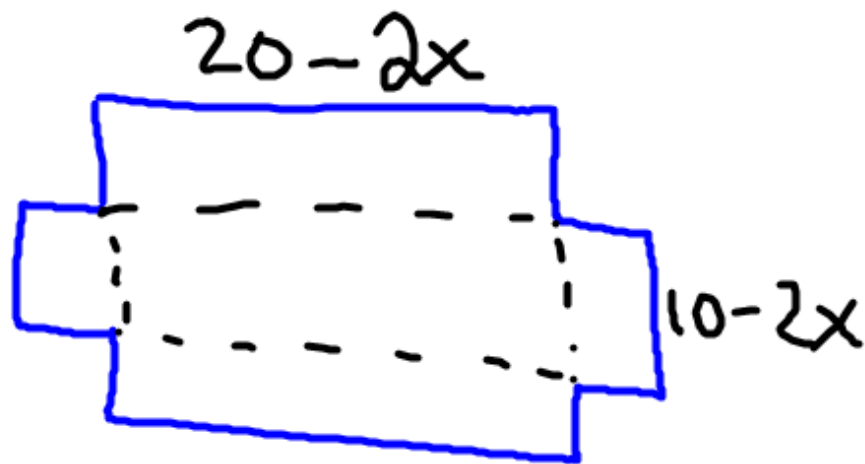


a) Length

$$20 - 2x$$

b) Width

$$10 - 2x$$



c) Area Base

$$(20 - 2x)(10 - 2x)$$

$$= 200 - 40x - 20x + 4x^2$$

$$= 4x^2 - 60x + 200$$



d) Volume Box

$$V = \underbrace{(20 - 2x)}_L \underbrace{(10 - 2x)}_W \underbrace{x}_H$$

$$V = (4x^2 - 60x + 200)x$$

$$V = 4x^3 - 60x^2 + 200x$$

Homework

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15, 17, 18b, 21

***I know it's a lot, but the best way to improve is to
PRACTICE PRACTICE PRACTICE!!!***